Non-competing Data Intermediaries

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Abstract

I study competition among data intermediaries—technology companies and data brokers that collect consumer data and sell them to downstream firms. When firms’ use of data hurts consumers, intermediaries need to compensate consumers for collecting their data. However, competition may not increase compensation: If intermediaries offer high compensation, consumers share data with multiple intermediaries, which lowers the price of data in the downstream market and hurts intermediaries. This leads to multiple equilibria: There is a monopoly equilibrium, and an equilibrium with greater data concentration benefits intermediaries and hurts consumers. I use my results to solve information design by data intermediaries.

Keywords: information markets, intermediaries, personal data, privacy

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1 Introduction

This paper studies competition among data intermediaries, which collect and distribute personal data between consumers and firms: Data brokers, such as LiveRamp and Nielsen, collect consumer data and sell them to retailers and advertisers (Federal Trade Commission, 2014). Technology companies, such as Google and Facebook, collect user data and share them indirectly through targeted advertising spaces. Mobile application developers collect user data and share them with third parties (Kummer and Schulte, 2019). I regard these companies as data intermediaries and study how they compete for personal data.

Specifically, consider consumers deciding whether to join online platforms, which collect personal data and share them with third parties. The use of data by third parties may benefit or hurt consumers. For example, it may hurt consumers through price discrimination, spam, and further data leakage. In this case, platforms need to provide consumers valuable services and rewards (e.g., social media) in order to obtain their data.

I model such a situation as a two-sided market for personal data. The main focus is the price-setting behavior of data intermediaries. On the one side, they set prices to obtain consumer data. Prices represent the quality of online services or rewards that consumers can enjoy in exchange for providing data. On the other side, intermediaries set prices to sell collected data to third parties.

The main question is whether competition among intermediaries dissipates their profits. The question is important for understanding how the surplus generated by data is allocated. In traditional markets, the answer to this question is often yes: The idea reminiscent of Demsetz (1968) suggests that intermediaries compete in the upstream market to have market power in the downstream market, and this competition drives their profits to zero. However, in the market for data, this may not be the case.

The model consists of consumers, data intermediaries, and downstream firms. In the upstream market, intermediaries collect data from consumers in exchange for compensation. In the downstream market, intermediaries post prices and sell collected data to firms. The set of data that each intermediary acquires in the upstream market depends on consumers’ data-sharing decision: Each consumer decides what data to share with each intermediary, balancing compensation it offers and the expected benefit or loss she will experience when downstream firms acquire her data.
One may think that competition incentivizes intermediaries to pay greater compensation to consumers. The key idea of the paper is that this may not occur. To see this, suppose that intermediaries offer consumers high compensations to obtain more data. Consumers then share their data with multiple intermediaries. This intensifies price competition and lowers the price of data in the downstream market, which hurts intermediaries. The economic force is driven by the non-rivalry of data: Unlike conventional economic goods, the same data can be simultaneously obtained and sold by any number of intermediaries.

I show that this economic force leads to multiple equilibria that differ in the set of data that each intermediary acquires. There are three main findings. First, when the use of data by downstream firms hurts consumers, there is a monopoly equilibrium in which one intermediary extracts the maximum possible surplus. Other intermediaries do not compensate consumers, because if they do, consumers will then share their data with multiple intermediaries. Thus, competition among data intermediaries may not dissipate their profits.

The second main finding is on data concentration, which refers to a small number of intermediaries acquiring a large amount of data. There are equilibria with different degrees of concentration. I show that if consumers incur the increasing marginal loss of sharing data with downstream firms, then data concentration benefits intermediaries and hurts consumers. This is because large intermediaries compensate consumers based on their infra-marginal loss. I also study the intensive and extensive margins of data concentration and show that they have different welfare implications.

The third main finding concerns a general case in which downstream firms’ use of data may hurt or benefit consumers, depending on the amount and type of data that firms acquire. I show that for arbitrary consumer preferences, there is a partially monopolistic equilibrium, in which intermediaries compete for some data but one intermediary acts as a monopolist for other data. As a result, intermediaries’ profits and consumer surplus fall between those under monopoly and competitive benchmark in which data are rivalrous.

I use this result to study information design by competing intermediaries. I assume that downstream firms use consumer data for price discrimination and product recommendation. Intermediaries can potentially obtain and sell any informative signals about consumers’ willingness to pay. In the partially monopolistic equilibrium, a single intermediary obtains a fully informative signal, with which firms can perfectly price discriminate and recommend the highest-value products to
consumers. I show that the equilibrium consumer surplus is equal to the one in (hypothetical) Bayesian persuasion where consumers directly disclose information to firms.

The paper helps us understand two issues of the data economy. One is why consumers do not seem to be compensated for providing their data (Arrieta-Ibarra et al., 2018; Carrascal et al., 2013). I show that the market for data could fail to reward consumers as suppliers of personal data. This explanation, which does not depend on consumer unawareness or the lack of transparency, could be important, because there has been increasing awareness of data sharing practices, and regulators have tried to ensure consumers’ control over data (e.g., the EU General Data Protection Regulation). The other issue is data concentration in the hands of major Internet platforms (e.g., Sokol and Comerford, 2015). I show that data concentration can arise even though data are non-rivalrous and the model excludes network externalities or returns to scale. Moreover, data concentration can hurt consumers by lowering compensation for data. This result has a potential implication on regulating dominant online platforms.

The rest of the paper is organized as follows. Section 2 discusses related works and Section 3 describes the model. Section 4 considers two benchmarks: One is the case of a monopoly intermediary, and the other is when data are rivalrous. Section 5 describes a unique equilibrium payoff in the downstream market. Section 6 assumes that consumers incur loss of sharing data with downstream firms. I show that there are multiple non-competitive equilibria. This section also studies the welfare impacts of data concentration. Section 7 generalizes these results by allowing general consumer preferences. This section also studies information design by competing intermediaries. Section 8 provides extensions, and Section 9 concludes.

2 Literature Review

This paper relates to two strands of literature. First, it relates to the recent literature on markets for data. Bergemann and Bonatti (2019) study under what condition a monopoly data intermediary can earn a positive profit by collecting and selling consumer data. They assume that a downstream firm uses data for price discrimination that hurts consumers. In contrast, I assume that the intermediation of data is profitable and focus on competition and data concentration.

More broadly, this paper relates to works on markets for data beyond the context of price dis-
discrimination. Gu et al. (2018) study data brokers’ incentives to merge data. While I mainly assume that a downstream firm’s revenue is a submodular function of data set, they consider supermodularity as well.\footnote{However, Proposition 3 shows that the main insight holds regardless of the shape of a firm’s revenue function.} In contrast to their work, I endogenize how intermediaries collect consumer data in the upstream market. This enables me to conduct consumer welfare analysis. Bergemann et al. (2018) consider a model of data provision and data pricing. Jones et al. (2018) study, among other things, how different property rights of data affect economic outcomes in a semi-endogenous growth model. Choi et al. (2018) consider consumers’ privacy choices in the presence of an information externality. Kim (2018) considers a model of a monopoly advertising platform and studies consumers’ privacy concerns, market competition, and vertical integration between the platform and sellers.

Second, the paper relates to the literature on platform competition in two-sided markets. The literature typically assumes that a transaction between two sides is mutually beneficial (e.g., Armstrong (2006); Caillaud and Jullien (2003); Rochet and Tirole (2003)). This is natural in many applications such as video games (consumers and game developers) and credit cards (cardholders and merchants). When a transaction is mutually beneficial, platform competition involves undercutting prices charged to at least one side, which is sustainable even if multi-homing is possible. In contrast, I assume that a transaction (i.e., a downstream firm’s acquiring data) benefits one side (i.e., a firm) but may benefit or hurt the other side (i.e., a consumer). When transaction hurts one side—that is, when downstream firms use data to extract rents from consumers—competition among intermediaries involves raising compensation for consumers. I show that such competition does not occur when multi-homing is possible, which is captured by the nonrivalry of data.

Caillaud and Jullien (2003) show that intermediaries have an incentive to make their services non-exclusive in order to relax price competition. Their result is logically distinct from mine. For instance, in their model, intermediaries earn positive (but below monopoly) profits only if matching technology is costly and imperfect. In my model, intermediaries can earn a monopoly profit without these frictions. Negative cross-side externalities also appear in models of advertising platforms, such as Anderson and Coate (2005) and Reisinger (2012). There, the presence of advertisers imposes negative externalities on users due to nuisance costs.
3 Model

There are $N \in \mathbb{N}$ consumers, $K \in \mathbb{N}$ data intermediaries, and a single downstream firm.\footnote{As I show in Section 8, this is equivalent to a model with multiple downstream firms that do not interact with each other.} Where it does not cause confusion, $N$ and $K$ denote the sets of consumers and intermediaries, respectively. Figure 1 depicts the game: Intermediaries obtain consumer data in the upstream market and sell them in the downstream market. The detail is as follows.

**Upstream Market**

Each consumer $i \in N$ has a finite set $D_i$ of data. Each element of $D_i$ is an indivisible and non-rivalrous good.\footnote{For example, $D_i = \{i$’s age, $i$’s email address, $i$’s income$\}$.} $D := \bigcup_{i \in N} D_i$ denotes the set of all data in the economy.

At the beginning of the game, each intermediary $k \in K$ simultaneously makes an offer $(D^k_i, \tau^k_i)_{i \in N}$. $\tau^k_i \in \mathbb{R}$ is the amount of compensation that intermediary $k$ is willing to pay for $i$’s data $D^k_i \subset D_i$. Compensation $\tau^k_i$ represents the quality of online services and monetary rewards. $\tau^k_i < 0$ is interpreted as a fee to transfer data. If $D^k_i \neq \emptyset$, I call $(D^k_i, \tau^k_i)$ a non-empty offer.

After observing offers, each consumer $i$ decides which offers to accept. Motivated by the non-rivalry of data, I impose no restriction on the number of offers consumers can accept. Formally, each consumer $i$ simultaneously chooses $K_i \subset K$, where $k \in K_i$ means that consumer $i$ provides data $D^k_i$ to intermediary $k$ and earns $\tau^k_i$. These decisions determine intermediary $k$’s data $D^k = \bigcup_{i \in K} D^k_i$.
∪_{i \in N^k} D^k$, where $N^k := \{i \in N : k \in K_i\}$ is the set of consumers who accept the offers from intermediary $k$. All intermediaries and the firm publicly observe $(D^1, \ldots, D^K)$, which I call the allocation of data. Given any $D^k \subset \mathcal{D}$, let $D^k_i := D^k \cap \mathcal{D}_i$ denote intermediary $k$’s data on consumer $i$.

**Downstream Market**

Given the allocation of data $(D^1, \ldots, D^K)$, each intermediary $k$ simultaneously posts a price $p^k \in \mathbb{R}$ for its data. The firm then chooses the set $K' \subset K$ of intermediaries, from which the firm buys data $D := \cup_{k \in K'} D^k$ at total price $\sum_{k \in K'} p^k$. Note that the firm obtains consumer $i$’s data $d_i \in \mathcal{D}_i$ if and only if there is $k \in K$ such that $d_i \in D^k_i$ and $k \in K_i \cap K'$. $d_i \in D^k_i$ means that intermediary $k$ asks for $d_i$, $k \in K_i \cap K'$ means that consumer $i$ accepts the offer of intermediary $k$ and the firm buys data from $k$.

**Preferences**

All players maximize expected payoffs, and their ex post payoffs are as follows. The payoff of each intermediary is revenue minus compensation: Suppose that intermediary $k$ pays compensation $\tau^k_i$ to each consumer $i \in N^k$ and posts a price of $p^k$, and the firm buys data from a set $K'$ of intermediaries. Then, intermediary $k$ obtains a payoff of $1_{\{k \in K'\}} p^k - \sum_{i \in N^k} \tau^k_i$, where $1_{\{x \in X\}}$ is the indicator function that is 1 or 0 if $x \in X$ or $x \not\in X$, respectively.

The payoff of each consumer is as follows. Suppose that consumer $i$ earns a compensation of $\tau^k_i$ from each intermediary in $K_i$, and the firm obtains her data $D_i \subset \mathcal{D}_i$. Then, $i$’s payoff is $U_i(D_i) + \sum_{k \in K_i} \tau^k_i$. The second term is the total compensation from intermediaries. The first term $U_i(D_i)$ is consumer $i$’s gross payoff when the firm acquires her data $D_i$ from intermediaries. For example, $U_i$ is a decreasing (set) function if the firm uses data to extract rents from consumers. I normalize $U_i(\emptyset) = 0$ and impose more structures later. Note that each consumer’s gross payoff is independent of other consumer’s data that the firm acquires. However, the results do not rely on this assumption (see Subsection 8.3 for the detail).

The payoff of the downstream firm is as follows. If the firm obtains data $D \subset \mathcal{D}$ and pays a total price of $p$, then the firm obtains a payoff of $\Pi(D) - p$. The first term is the firm’s revenue from data $D$. The firm benefits from data but the marginal revenue is decreasing:

**Assumption 1.** $\Pi : 2^\mathcal{D} \to \mathbb{R}_+$ satisfies the following.
1. \( \Pi(D) \) is increasing in \( D \): For any \( X, Y \subset D \) such that \( X \subset Y \), \( \Pi(Y) \geq \Pi(X) \).

2. \( \Pi(D) \) is submodular in \( D \): For any \( X, Y \subset D \) with \( X \subset Y \) and \( d \in D \setminus Y \), it holds

\[
\Pi(X \cup \{d\}) - \Pi(X) \geq \Pi(Y \cup \{d\}) - \Pi(Y).
\]

(If inequality (1) is strict for any \( X \subsetneq Y \), \( \Pi_i \) is strictly submodular.)

3. \( \Pi(\emptyset) = 0 \).

Submodularity is motivated by the idea that data typically exhibit decreasing returns to scale (Varian, 2018). However, Section 7 considers any increasing \( \Pi \).

**Timing and Solution Concept**

The timing of the game, depicted in Figure 1, is as follows. First, each intermediary simultaneously makes an offer to each consumer. Second, each consumer simultaneously decides the set of offers to accept. The decision of each consumer determines the allocation of data. Then, each intermediary simultaneously posts a price to the firm. Finally, the firm chooses the set of intermediaries from which it buys data. The solution concept is pure-strategy subgame perfect equilibrium in which each consumer’s data-sharing decision depends only on offers to her and not on offers to other consumers. This restriction ensures that equilibria I consider are not sensitive to each consumer’s information about other consumers’ offers.

**3.1 Applications**

Before proceeding to the analysis, I present three applications.

**Online Platforms**

We may view data intermediaries as online platforms such as Google and Facebook. The model captures the following situation: Platforms provide online services to consumers in exchange for their data. \( D_i^k \) represents the set of data that consumers need to provide to use platform \( k \), and \( \tau_i^k \) represents the quality of \( k \)’s service. Platforms may share data with third parties, such as advertisers, retailers, and political consulting firms. Data sharing with each third party can benefit
(e.g., better targeting) or hurt (e.g., price discrimination and privacy concern) a data subject. The aggregate impact of these effects is summarized by $U_i(D_i)$.

Several remarks are in order. First, the model assumes that $U_i(\cdot)$ is exogenous, that is, intermediaries cannot directly influence how the firm’s use of data affects consumers. This reflects the difficulty of writing a fully contingent contract over how and which third parties can use personal information. The lack of commitment over the sharing and use of data plays an important role in other models of markets for data such as Huck and Weizsacker (2016) and Jones et al. (2018).

Second, the model formulates compensation as one-to-one transfer. This is mainly to simplify the analysis; the results continue to hold even if the cost of compensating consumers is non-linear. The assumption of costly compensation is natural if compensation is monetary transfer or an intermediary needs to invest to improve the quality of its service.

Third, I assume that the benefit for consumer $i$ of sharing data with intermediary $k$ depends only on $\tau_i^k$. However, if we interpret intermediaries as online platforms, we may think that the benefit should increase if other consumers provide more data (e.g., social media). I deliberately exclude such a situation to clarify that the results are not driven by network externalities or returns to scale.

Finally, the model abstracts from the institutional details of online advertising platforms. For instance, they distribute personal data indirectly through sponsored search or targeted display advertising. For another instance, they compete for not only data but also the attention of consumers. Nonetheless, by regarding these platforms as pure data intermediaries, I can isolate a novel economic mechanism potentially relevant to their competition.

**Data Brokers**

We can interpret intermediaries as data brokers such as LiveRamp, Nielsen, and Oracle. The business model of these firms is to collect personal information from online and offline sources, and resell or share that information with others such as retailers and advertisers (Federal Trade Commission, 2014).

Some data brokers obtain data from consumers in exchange for monetary compensation (e.g., Nielsen Home Scan). However, data brokers commonly obtain personal information without interacting with consumers. The model could also fit such a situation. For example, suppose that
data brokers obtain individual purchase history from retailers. Consider the following chain of transactions: Retailers compensate customers and record their purchases. For example, retailers may offer discounts to customers who sign up for loyalty cards. Retailers then sell these records to data brokers, which resell the data to downstream firms. We can regard retailers in this example as consumers in the model.

Alternatively, the model can be useful for understanding how the incentives of data brokers would look like if they had to source data directly from consumers. The question is of growing importance, as awareness of data sharing practices increases and policymakers try to ensure that consumers have control over their data (e.g., The EU General Data Protection Regulation and California Consumer Privacy Act).

**Mobile Application Industry**

The model fits a market for mobile applications. Kummer and Schulte (2019) empirically show that mobile app developers trade greater access to personal information for lower app prices, and consumers choose between lower prices and greater privacy when they decide which apps to install. Moreover, app developers share collected data with third parties for direct monetary benefit (see Kummer and Schulte 2019 and references therein). The model captures such economic interactions as a two-sided market for consumer data. We may think that competition encourages app developers to “pay” more for consumer data in the form of lower app prices and higher qualities. I will show that this may not be the case because paying more for consumer data makes data worth less in the downstream market.

**4 Preliminary Analysis**

This section provides two benchmarks, which I will compare with the main specification.

**4.1 Monopoly Intermediary**

Consider a monopoly data intermediary \((K = 1)\). For any set of data \(D \subset D\), I write consumer \(i\)’s gross payoff \(U_i(D \cap D_i)\) as \(U_i(D)\). Suppose that the monopolist obtains and sells data \(D\). If
$U_i(D) < 0$, consumer $i$ requires compensation of at least $-U_i(D)$; If $U_i(D) > 0$, she is willing to pay up to $U_i(D) > 0$ for her data to be transferred. The firm is willing to pay up to $\Pi(D)$ for the data. Thus, I obtain the following result.

**Claim 1.** A monopoly data intermediary maximizes and extracts total surplus. Formally, in any equilibrium, a monopoly intermediary obtains and sells data $D^M \subset D$ that satisfies

$$D^M \in \arg \max_{D \subset D} \Pi(D) + \sum_{i \in N} U_i(D). \quad (2)$$

All consumers and the firm obtain zero payoffs.

Later, I use $D^M$ to describe equilibria with multiple intermediaries. If the right hand side of (2) has multiple maximizers, I pick one of them arbitrarily as $D^M$ and conduct the analysis.

### 4.2 Competition for Rivalrous Goods

Suppose that data are rivalrous—each consumer can provide each piece of data to at most one intermediary.$^4$ Such a model corresponds to the market for conventional economic goods.$^5$ In this case, competition among intermediaries dissipates profits and enables consumers to extract full surplus (see Appendix A for the proof).

**Claim 2.** Suppose that data are rivalrous and there are multiple intermediaries. In any equilibrium, all intermediaries and the firm obtain zero payoffs. If $\Pi$ is strictly supermodular, in any equilibrium, there is at most one intermediary that obtains non-empty data.

Intermediaries make zero profit due to Bertrand competition in the upstream market: If one intermediary earned a positive profit by obtaining data $D^k$, then another intermediary could profitably deviate by offering consumers slightly higher compensation to exclusively obtain $D^k$. For such a deviation to be unprofitable, no intermediary can earn a positive profit in equilibrium.

$^4$Formally, I assume that each consumer $i$ can accept a collection of offers $(D^k_i, \tau^k_i)_{k \in K_i}$ if and only if $D^k_i \cap D^j_i = \emptyset$ for any distinct $j, k \in K_i$.

$^5$This model is similar to Stahl (1988), who shows that competition among intermediaries for physical goods can lead to a Walrasian outcome.
5 Equilibrium Analysis: Downstream Market

Hereafter, I consider the main specification: Multiple intermediaries buy and sell non-rivalrous data. First, I show that the equilibrium revenue of each intermediary in the downstream market is unique and equal to the marginal contribution of its data to the firm’s revenue. The result relies on the submodularity of the firm’s revenue function $\Pi$.

Lemma 1. Suppose that each intermediary $k$ holds data $D^k$. In any equilibrium of the downstream market, intermediary $k$ obtains a revenue of

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\Pi^k := \Pi \left( \bigcup_{j \in K} D^j \right) - \Pi \left( \bigcup_{j \in K \setminus \{k\}} D^j \right),
$$

and the firm obtains data $\bigcup_{k \in K} D^k$.

Proof. I show that there is an equilibrium (of the downstream market) in which each intermediary $k$ posts a price of $\Pi^k$ and the firm buys all data. First, the submodularity of $\Pi$ implies that $\Pi(\bigcup_{k \in K' \cup \{j\}} D^j) - \Pi(\bigcup_{k \in K'} D^j) \geq \Pi^j$ for all $K' \subset K$. Thus, if each intermediary $k$ sets a price of $\Pi^k$, the firm prefers to buy all data. Second, if intermediary $k$ increases its price, the firm strictly prefers buying data from intermediaries in $K \setminus \{k\}$ to buying data from a set of intermediaries containing $k$. Finally, if an intermediary lowers the price, it earns a lower revenue. Thus, no intermediary has a profitable deviation. The uniqueness of the equilibrium revenue is relegated to Appendix B.

Lemma 1 has two implications. First, consumers anticipate that any data they share with intermediaries will be sold to the downstream firm. Second, intermediaries earn zero revenue in the downstream market if they hold the same data. This is similar to Bertrand competition with homogeneous products. More generally, the revenue of an intermediary depends only on the part of the data that other intermediaries do not hold.

Corollary 1. Suppose that each intermediary $j \neq k$ holds data $D^j$. The equilibrium revenue of

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6Lerner and Tirole (2004) focus on a symmetric environment but do not assume submodularity. Gu et al. (2018) assume $K = 2$ and consider both submodularity and supermodularity. The uniqueness of the equilibrium revenue is a new result.
intermediary $k$ in the downstream market is identical between when it holds $D^k$ and $D^k \cup D'$, where $D'$ is any subset of $\bigcup_{j \neq k} D^j$.

6 Consumers with Costly Data Sharing

Given Lemma 1, I describe equilibria of the entire game. To illustrate the main idea in a simply way, this section assumes that $U_i(D_i)$ is decreasing in $D_i$, that is, each consumer obtains a lower payoff if she shares a greater set of data with the firm.

6.1 Consumers with Single Unit Data

I begin with the simplest case in which each consumer $i$ has single unit data and her payoff decreases by $C_i$ if the firm acquires her data.

Assumption 2. For each $i \in N$, $D_i = \{d_i\}$ and $C_i := -U(\{d_i\}) > 0$.

A motivation for this assumption is that the harmful use of personal data by third parties has been actively discussed by policymakers as a key issue of online privacy problems (Federal Trade Commission, 2014). $C_i$ should be thought of as a reduced form capturing a consumer’s loss from, say, price discrimination, privacy concern, and intrusive marketing campaign.

The following notion simplifies the exposition.

Definition 1. The allocation of data $(D^1, \ldots, D^K)$ is partitional if no two intermediaries obtain the same piece of data: $D^k \cap D^j = \emptyset$ for all $k, j \in K$ with $k \neq j$.

The following result states that although data are non-rivalrous, no two intermediaries obtain the same piece of data on the equilibrium path (see Appendix C for the proof).

Proposition 1. In any equilibrium, the allocation of data is partitional.

Intuitively, if two intermediaries obtained the same data, one of them could increase a profit by not collecting the data: The deviation does not change its revenue in the downstream market (Lemma 1) but reduces compensation to consumers.

Proposition 1 resembles product differentiation. As products in this model are consumer data, intermediaries’ incentives for product differentiation affect consumer surplus. The following result
illustrates this point: It presents equilibria in which consumer surplus and total surplus are equal to the monopoly outcome. Recall that $D^M$ is the set of data that a monopoly intermediary acquires (see Appendix D for the proof).

**Theorem 1.** Take any partitional allocation of data $(D^1, \ldots, D^K)$ with $\bigcup_{k \in K} D^k = D^M$. Then, there is an equilibrium with the following properties.

1. The equilibrium allocation of data is $(D^1, \ldots, D^K)$.

2. Consumer surplus is zero: In the upstream market, intermediary $k$ pays consumer $i$ a compensation of $1_{\{d \in D^k\}} C_i$.

3. In the downstream market, each intermediary $k$ obtains a revenue of  
\[ \Pi(D^M) - \Pi(D^M \setminus D^k). \]

The theorem states that any partition of $D^M$, the set of data that a monopolist would acquire, can arise as an allocation of data. For example, different intermediaries may specialize in acquiring different kinds of data. However, consumer surplus is zero across all of these equilibria. In contrast, intermediaries and the downstream firm may obtain different payoffs across these equilibria (Section 6.3 studies this point in detail).

The intuition for Theorem 1 is as follows. Take any equilibrium described above, and consider an intermediary’s incentive to deviate. For example, suppose that intermediary 1 deviates and offers positive compensation to consumers for data $D^2$, which intermediary 2 is going to acquire. Then, these consumers will provide their data to not only intermediary 1 but 2. Indeed, when consumers share data with one intermediary, they also prefer to share data with other intermediaries that offer positive compensation: By doing so, consumers can earn higher total compensation without increasing the loss from the firm’s use of data.\footnote{As I show in Section 8, this argument is not specific to the assumption that consumers do not incur (exogenous) loss from sharing data with intermediaries.} However, if consumers share data with intermediaries 1 and 2, these intermediaries cannot charge a positive price for data $D^2$ in the downstream market. Anticipating this, intermediary 1 prefers to not compensate for any data in $D^2$. Since each intermediary faces no competing offers, it can acquire data at the monopsony price.
Ci. Also, intermediaries have no incentive to acquire data in \( D \setminus D^M \) because consumers ask for greater compensation than the price of their data in the downstream market.

The non-rivalry of data is important not only for consumers’ receiving zero surplus (Point 2) but also for the multiplicity of allocations of data. By Claim 2, if data were rivalrous, a mild condition guarantees that at most one intermediary acquires non-empty data.

Theorem 1 implies that there is a monopoly equilibrium. Thus, the presence of multiple intermediaries may not dissipate their profits:

**Theorem 2.** For any number of intermediaries in the market, there is an equilibrium in which a single intermediary acts as a monopolist described in Claim 1.

**Proof.** Take \( D^k = D^M \) and \( D^j = \emptyset \) for all \( j \neq k \) in Theorem 1.

The results have policy and antitrust implications. First, data portability under the European General Data Protection Regulations might lower consumer welfare. Data portability states that data controller, such as online platforms, must allow consumers to withdraw and transfer their data across competitors. Let us interpret the models of non-rivalrous and rivalrous data as the economy with and without data portability, respectively. Then, the comparison of Theorem 2 with Claim 2 implies that data portability could relax ex ante competition for data and transfer surplus from consumers to intermediaries. It would be interesting to examine the welfare impact of data portability by incorporating this potential downside and the intended benefit of preventing consumer lock-in, which the current model does not capture.⁸

Second, market concentration might not be a right measure of market power that data intermediaries hold against producers of personal data—consumers. Theorem 1 implies that many intermediaries obtaining small pieces of data are consistent with consumers obtaining zero surplus. Indeed, such a situation transfers surplus from intermediaries to downstream firms, not to consumers. This is because for any allocation of data, each intermediary acts as a monopsony of each piece of data.

**Remark 1 (Observability of the Allocation of Data).** It is crucial for my analysis that the allocation of data is publicly observable. In other words, I assume that intermediaries know what data other intermediaries hold. I adopt such an assumption for two reasons.

²⁸Krämer and Stülele (2019) study a model in which consumers’ switching costs depend on data portability.
First, in practice, data intermediaries seem to provide information about what kind of data they collect. For example, a data broker CoreLogic states that it holds property data covering more than 99.9% of U.S. property records.\(^9\) Also, if an intermediary collects data directly from consumers, then it needs to communicate to consumers what data it collects, which would also be observable to other intermediaries (e.g., Nielsen Homescan).

Second, intermediaries have an incentive to make the allocation of data observable, because it makes intermediaries better off in the Pareto sense. Indeed, if each intermediary privately observes its data, then in any equilibrium, all intermediaries obtain zero payoffs. To see this, suppose to the contrary that intermediary \(k\) earns a positive profit, which implies that \(k\) sells non-empty data at a positive price to the firm. Then, intermediary \(k\) can profitably deviate by not collecting any data in the upstream market and charges the same price in the downstream market. The deviation profits \(k\) because the firm cannot detect such a deviation. Alternatively, we could think of a situation in which the data held by each intermediary is observable to the firm but not to other intermediaries. However, such a setting is intractable because there is no pure-strategy equilibrium.\(^10\)

**Remark 2.** The existence of the monopoly equilibrium (Theorem 2) is robust to a variety of extensions. For example, consumers could incur exogenous costs of sharing data with intermediaries (e.g., privacy concern); \(U_i\) could depend on what data other consumers share with the firm (e.g., downstream firms use consumer \(j\)’s data to predict the characteristics of consumer \(i\)); intermediaries could incur heterogeneous costs of processing and storing data. Section 7 and Section 8 discuss some of them in detail.

**Remark 3.** It is natural to ask whether there are equilibria other than those in Theorem 1. The answer is yes: The following example shows that both consumer surplus and total surplus can be different from the monopoly outcome.

**Example 1.** Consider a single consumer and two intermediaries. There is an equilibrium in which the consumer extracts full surplus \(\Pi(d_1) - C_1\): One intermediary, say 1, offers \((\{d_1\}, \Pi(d_1))\), and the other intermediary offers \((\{d_1\}, 0)\). On the path of play, the consumer accepts only


\(^{10}\)Suppose that there is a pure-strategy equilibrium in which the firm acquires non-empty data \(D\). Then, some intermediary \(k\) can profitably deviate by obtaining data \(D\) for free from consumers and setting a slightly lower price than how much the firm would pay without \(k\)’s deviation. Note that other intermediaries cannot detect such a deviation.
If intermediary 1 unilaterally deviates and lowers compensation to $\tau_1^1$ such that $C_1 < \tau_1^1 < \Pi(d_1)$, then the consumer accepts offers of both intermediaries. This consists of an equilibrium. In particular, intermediary 1 has no incentive to lower compensation, because the consumer will then share her data with all intermediaries.

There is also an equilibrium in which no data are shared. On the path of play, both intermediaries offer $(\{d_1\}, 0)$ and the consumer rejects them. If an intermediary unilaterally deviates and offer $(\{d_1\}, \tau)$ with $\tau \geq C_1$, the consumer accepts offers of both intermediaries. This consists of an equilibrium. In particular, no intermediary has an incentive to obtain data, because the consumer will then share her data with all intermediaries, following which the price of the data is zero.

A common feature of these equilibria is that a consumer punishes a deviating intermediary 1 by disseminating her data $d_1$ with multiple intermediaries. This is possible because intermediary 2 also asks for $d_1$ at compensation between zero and $C_1$. Note that the consumer is indifferent between accepting and rejecting the offer from intermediary 2, conditional on her accepting the offer from intermediary 1. However, on the equilibrium path, the consumer has to reject the offer from intermediary 2: If she accepted, intermediary 1 would prefer to not compensate for data $d_1$ that would be valueless in the downstream market.

The paper does not focus on these equilibria for two reasons. First, the purpose of this paper is not to characterize all equilibria but to provide an intuition for why multiple homogeneous intermediaries can sustain non-competitive outcomes. The equilibria described in Example 1 do not fit this purpose because they seem to be sustained by a different economic mechanism.

Second, I aim to study how the market structure of data intermediaries affects the allocation of surplus created by data. As a first step, it is reasonable to focus on equilibria with the same total surplus and study how this surplus is divided.

### 6.2 Consumers with Multidimensional Data

In the following analysis, I generalize Theorems 1 and 2 by relaxing assumptions on consumer preferences. Assume now that each consumer $i$ has any finite set $D_i$ of data and that consumers incur increasing convex costs of sharing data.

**Assumption 3.** For each $i \in N$, the cost of sharing data $C_i := -U_i$ satisfies the following.
1. $C_i(D_i)$ is increasing in $D_i$: For any $X, Y \subset D_i$ such that $X \subset Y$, $C_i(Y) \geq C_i(X)$.

2. $C_i(D_i)$ is supermodular in $D_i$: For any $X, Y \subset D_i$ with $X \subset Y$ and $d \in D_i \setminus Y$, it holds that

$$C_i(Y \cup \{d\}) - C_i(Y) \geq C_i(X \cup \{d\}) - C_i(X).$$

(4)

This setting involves a new challenge: The equilibria in Theorem 1 have a simple and nice property that each intermediary $k$ asks consumer $i$ for data $D^k_i$ and consumers accept all non-empty offers. In contrast, the current setting may not have such an equilibrium.\textsuperscript{11} To avoid this difficulty, I focus on an environment where Theorem 1 naturally extends.

**Assumption 4.** Total surplus is maximized when the firm acquires all data, i.e., $D^M = D$.\textsuperscript{12}

Assumption 4 holds, for example, if a downstream firm uses data for price discrimination, and the firm can perfectly price discriminate by using all data $D$. Subsection 7.2 microfound $U_i$ and $\Pi$ using this interpretation. In terms of the primitives, the assumption holds if the firm’s marginal revenue from data is high relative to consumers’ marginal costs of sharing the data. For example, for any $\Pi$ and $(C_i)_{i \in N}$, the assumption holds if the firm’s revenue function is $\alpha \Pi$ with a large $\alpha > 1$. Under Assumption 4, Theorem 1 extends (see Appendix E for the proof).

**Theorem 3.** Take any partitional allocation of data $(D^1, \ldots, D^K)$ with $\cup_{k \in K} D^k = D^M$. Then, there is an equilibrium with the following properties.

1. The equilibrium allocation of data is $(D^1, \ldots, D^K)$.

2. In the upstream market, intermediary $k$ acquires consumer $i$’s data $D^k_i$ at compensation $\hat{\tau}^k_i$, which is the marginal cost of sharing $D^k_i$:

$$\hat{\tau}^k_i := C_i(D_i) - C_i(D_i \setminus D^k_i).$$

(5)

\textsuperscript{11}Formally, this general setting may not have an equilibrium that reduces to the one in Theorem 1 when I assume that each consumer has single unit data.

\textsuperscript{12}Recall that the monopoly intermediary extracts total surplus, and thus it acquires data $D^M$ to maximize total surplus.
3. In the downstream market, each intermediary \( k \) obtains a revenue of

\[
\hat{p}^k := \Pi(D) - \Pi(D \setminus D^k).
\]

(6)

In particular, there is an equilibrium in which a single intermediary acts as a monopolist.

A key difference from the case of single unit data (Theorem 1) is the equilibrium compensation. Point 2 of Theorem 3 states that intermediary \( k \) compensates consumer \( i \) according to the additional loss that consumer \( i \) incurs by sharing \( D_i^k \) conditional on sharing data with other intermediaries \( j \neq k \). If \( C_i \) is not additively separable, this creates a wedge between the total compensation \( \sum_{k \in K} \hat{r}_i^k \) and the cost \( C_i(D_i) \).

To have a better intuition, consider the following example. Each consumer has her location and financial data. The downstream firm profits from data but there is a risk of data leakage. Each consumer incurs an expected loss of $20 from this potential data leakage if only if the firm holds both location and financial data (otherwise, she incurs no loss). Theorem 3 implies that there are at least two equilibria: In one, intermediaries 1 and 2 specialize in acquiring location and financial data, respectively, and each intermediary pays each consumer a compensation of $20. For example, two intermediaries may operate different mobile applications that collect different data, and each application delivers the value of $20 to consumers. In this equilibrium, each consumer obtains a net surplus of $20. In the other equilibrium, intermediary 1 acquires both location and financial data and pays $20, leaving zero surplus to consumers. Thus, consumer surplus is lower at the equilibrium in which a single intermediary obtains both location and financial data. The following subsection generalizes this observation.

6.3 Welfare Impacts of Data Concentration

Theorems 1 and 3 state that any partition of \( D^M \) can arise as an equilibrium allocation of data. We can interpret an equilibrium corresponding to a coarser partition as an equilibrium with a greater data concentration among intermediaries. The following definition formalizes this idea:

**Definition 2.** Take two partitional allocations of data, \((D^k)\) and \((\hat{D}^k)\). We say that \((\hat{D}^k)\) is *more concentrated than* \((D^k)\) if (i) \( \cup_{k \in K} D^k = \cup_{k \in K} \hat{D}^k \) and (ii) for each \( k \in K \), there is \( \ell \in K \) such
that $D^k \subset \hat{D}^\ell$.

The following result summarizes the impact of data concentration on consumers and intermediaries (see Appendix F for the proof).

**Theorem 4.** Data concentration benefits intermediaries and may hurt consumers:

1. Consider equilibria in Theorem 1. Intermediaries’ total profit is higher in an equilibrium with a more concentrated allocation of data.

2. Consider equilibria in Theorem 3. Consumer surplus is lower and intermediaries’ total profit is higher in an equilibrium with a more concentrated allocation of data.

The intuition is as follows. As in Lemma 1, the price of data $D^k$ is $\Pi(\bigcup_{j \in K} D^j) - \Pi(\bigcup_{j \in K \setminus \{k\}} D^j)$, the additional revenue the firm can earn from $D^k$ conditional on having other data. If there are many intermediaries each of which has a small part of $D^M$, then the contribution of each piece of data is close to the marginal revenue $\Pi(D^M) - \Pi(D^M \setminus \{d\})$. In contrast, if a few intermediaries hold a large fraction of $D^M$, the contribution of each data set is large. Thus, each intermediary can set a high price to extract the infra-marginal value of its data. Since $\Pi(\cdot)$ is submodular, the latter leads to a greater total revenue for intermediaries. Symmetrically, if a consumer’s cost $C_i$ is supermodular, data concentration hurts consumers. This is because a large intermediary can compensate consumers for their data according to the infra-marginal cost.

### 6.4 Intensive and Extensive Margins of Data Concentration

The allocation of data can be more concentrated at the intensive or extensive margin. To see this, consider the following example. There are two intermediaries. The left block of Figure 2 depicts a situation in which intermediary 1 obtains location data on all consumers in the US and EU, and intermediary 2 obtains financial data on all consumers in the US and EU. The right block of Figure 2 is an alternative allocation where intermediary 1 holds location and financial data on consumers in the US, and intermediary 2 obtains location and financial data on consumers in the EU. The allocation of data in the right block is more concentrated at the intensive margin, because each intermediary has more data about each data subject.
Next, suppose that there are four intermediaries. The left block of Figure 3 depicts a situation in which intermediaries 1 and 3 acquire location data on consumers in the US and EU, respectively, and intermediaries 2 and 4 acquire financial data on consumers in the US and EU, respectively. Suppose that intermediaries 1 and 3 merge. The right block of Figure 3 depicts such a situation where the new intermediary is labeled as 1. After the merger, the allocation of data becomes more concentrated at the extensive margin, because the new intermediary has location data on wider population.

The following definition generalizes these examples.

**Definition 3.** Let \((D^k)_k\) and \((\hat{D}^k)_k\) denote two partitional allocations of data with \(\cup_k D^k = \cup_k \hat{D}^k\).

1. \((\hat{D}^k)_k\) is more concentrated than \((D^k)_k\) at the intensive margin if for any given \(i \in N\) and any \(k \in K\), there is \(\ell \in K\) such that \(D^k_i \subset \hat{D}^\ell_i\).

2. \((\hat{D}^k)_k\) is more concentrated than \((D^k)_k\) at the extensive margin if \((\hat{D}^k)_k\) is more concentrated than \((D^k)_k\), and for any \(i \in N\) and any \(k \in K\), there is \(\ell\) such that \(D^k_i = \hat{D}^\ell_i\).

**Proposition 2.** Consider equilibria described in Theorem 3.
1. Data concentration at the intensive margin lowers consumer surplus. The impact on intermediaries’ total profit is ambiguous.

2. Data concentration at the extensive margin increases intermediaries’ total profit, and it does not affect consumer surplus.

Data concentration at the intensive margin does not necessarily imply data concentration in Definition 2. In Figure 2, \((\hat{D}_i^k)\) is more concentrated at the intensive margin but does not satisfy Definition 2. Indeed, intermediaries’ total profits could be higher or lower at \((\hat{D}_i^k)\) than \((D_i^k)\) depending on the shape of the firm’s revenue function \(\Pi\). For example, suppose that \(\Pi\) is separable across consumers, and the revenue function for each consumer is submodular. Then, concentration at the intensive margin leads to higher profits of intermediaries. In contrast, if the firm’s revenue function \(\Pi\) is separable across data, then concentration at the intensive margin might reduce intermediaries’ profits. In the example of location and financial data, intermediaries’ profits may decrease if the firm’s revenue is the sum of revenue from location data and revenue from financial data, each of which is a submodular set function.

7 Consumers with General Preferences

This section substantively relaxes the assumptions on preferences. First, I allow consumers and the firm to have any \(U_i\) and any increasing \(\Pi\), respectively. I show that there is a partially monopolistic equilibrium, which generalizes the monopoly equilibrium in Theorem 2. Second, if \(U_i\) is any submodular function, then any partition of \(D^M\) can arise as an equilibrium allocation of data, which generalizes Theorem 3. Finally, I use the results to study information design by competing intermediaries.

7.1 Partially Monopolistic Equilibrium and Other Generalizations

I continue to assume that there are multiple intermediaries and maintain Assumption 4. The following result generalizes Theorem 1 (see Appendix G for the proof).

**Proposition 3 (Partially Monopolistic Equilibrium).** Suppose that each \(U_i\) is any set function and \(\Pi\) is any increasing set function. There is an equilibrium in which a single intermediary
obtains all data and pays a compensation of $\max_{D \subset D_i} U_i(D) - U_i(D_i)$ to each consumer $i$, who obtains an equilibrium payoff of $\max_{D \subset D_i} U_i(D)$.

Suppose that consumer $i$ prefers to share some data with the firm for free, i.e., $\max_{D \subset D_i} U_i(D) > U_i(\emptyset) = 0$. Proposition 3 implies that consumer surplus is then greater than in the monopoly market (Claim 1) but lower than in the market with rivalrous goods (Claim 2). Thus, in general, competition among data intermediaries benefits consumers relative to monopoly, however, the benefit may be lower than in traditional markets with rivalrous goods.

To see why competition benefits consumers when $U_i^* := \max_{D \subset D_i} U_i(D) > 0$, consider a special case in which consumer $i$ prefers to share all data for free, i.e., $U_i^* = U_i(D_i)$. A monopoly intermediary extracts full surplus from consumer $i$ by charging a fee of $U_i^* > 0$. In contrast, if there are multiple intermediaries and intermediary $k$ charges a positive fee, then another intermediary $j \neq k$ can offer a slightly lower fee to exclusively obtain data from consumer $i$. Indeed, consumer $i$ has no incentive to accept the offer of intermediary $k$, because she can enjoy a benefit of $U_i^*$ as long as intermediary $j$ transfers her data. Thus, if intermediaries offer non-negative fees, consumer $i$ can credibly share her data with at most one intermediary. Then, Bertrand competition lowers the equilibrium fees down to zero. However, competition does not force intermediaries to offer positive compensation (i.e., negative fees). Due to the non-rivalry of data, once intermediaries offer positive compensation, consumers share data with all of them, which will hurt intermediaries.

Proposition 3 states that the above intuition applies to arbitrary preferences of consumers. Consider Figure 4, which assumes that $U_i$ depends only on the amount of data that the firm acquires. First, the monopoly intermediary obtains all data at a compensation of $-U_i(D_i)$ (short dotted arrow). The monopoly compensation $-U_i(D_i)$ consists of two parts: The monopolist extracts surplus created by $D_i^* \in \arg \max_{D \subset D_i} U_i(D)$ from consumer $i$ by charging $U_i(D_i^*) > 0$, and it obtains additional data $D_i \setminus D_i^*$ at the minimum compensation $U_i(D_i^*) - U_i(D_i)$ (long dotted arrow). In contrast, when there are multiple intermediaries, competition prevents intermediaries from extracting surplus $U_i(D_i^*)$. This guarantees that each consumer $i$ obtains a payoff of at least $U_i(D_i^*)$. However, competition does not increase compensation for data $D_i \setminus D_i^*$, the sharing of which hurts consumer $i$. To sum up, in the partially monopolistic equilibrium, a single intermediary acquires all data and compensates consumers according to the loss $U_i(D_i^*) - U_i(D_i)$ of sharing $D_i \setminus D_i^*$. 

23
We can view the partially monopolistic equilibrium as a generalization of the monopoly equilibrium (Theorem 2) in two ways. First, if $D_i = \{d_i\}$ and $U_i(d_i) < 0$, then the equilibrium coincides with the monopoly equilibrium. Second, if the market consists of many intermediaries, then the partially monopolistic equilibrium minimizes consumer surplus and maximizes the sum of profits of all intermediaries (see Appendix H for the proof):

**Proposition 4.** Suppose that $\Pi$ is strictly increasing. For a sufficiently large number $K$ of intermediaries, the partially monopolistic equilibrium in Proposition 3 minimizes consumer surplus and maximizes intermediary surplus across all equilibria.

The intuition is as follows. Suppose that in equilibrium, consumer $i$ obtains a payoff of $U_i(D_i^*) - \delta$ with $\delta > 0$. Then, any intermediary can exclusively obtain a (potentially subset of) data $D_i^*$ by offering $(D_i^*, \varepsilon)$ with $\varepsilon < \delta$. Such a deviation guarantees that each intermediary earns a positive payoff in equilibrium. I prove that the payoff from the deviation is bounded from below by a positive value that is independent of the number $K$ of intermediaries. This is a contradiction because as $K$ grows large, the payoff of some intermediary has to go to zero.

Next, consider Theorem 3, which shows that any partition of $D = D$ can arise as an equilibrium allocation of data. The following result generalizes the result for any submodular $U_i$ (see Appendix I for the proof).
Proposition 5. Suppose that each $U_i$ is submodular and there are $K = 2J$ intermediaries. Take any partitional allocation of data $(D_1, \ldots, D_J)$ for $J$ intermediaries with $\bigcup_{k=1}^{J} D^k = \mathcal{D}$. There is an equilibrium in which intermediary $k \leq J$ obtains $D^k$ and pays a compensation of

$$L_i(D^k_i) := \max \left\{ \max_{D \subset D_i} U_i(D) - U_i(D \cup D^k_i), 0 \right\}. \quad (7)$$

to each consumer $i$.

In this equilibrium, intermediary $k$ compensates consumer $i$ for $D^k_i$ according to the maximum loss that she could incur by sharing $D^k_i$, where the maximum is taken across all possible data other than $D^k_i$ that she could share with the firm. If $U_i$ is decreasing, then submodularity implies $L_i(D^k_i) = U_i(D \setminus D^k_i) - U_i(D)$, which is equal to the equilibrium compensation in Theorem 3. If $U_i$ is non-monotone, then $L_i(D^k_i)$ could be different from the actual loss that $i$ incurs by sharing $D^k_i$. If $D^k = \mathcal{D}$ for a unique $k$ and $D^j = \emptyset$ for any other $j \neq k$, then the equilibrium coincides with the partially monopolistic equilibrium.

Finally, the submodularity of $U_i$ implies that data concentration hurts consumers and benefits intermediaries, which generalizes Proposition 4.

Proposition 6. Consider equilibria in Proposition 5. An equilibrium with a greater data concentration (i.e., coarser partition) is associated with lower consumer surplus and greater intermediary surplus.

Proof. Take any disjoint sets $X, Y \subset \mathcal{D}_i$. Let $D^* \in \arg \max_{D \subset \mathcal{D}_i} U_i(D) - U_i(D \cup X \cup Y)$. The submodularity of $U_i$ implies that

$$U_i(D^* \cup X \cup Y) + U_i(D^*) \leq U_i(D^* \cup X) + U_i(D^* \cup Y)$$

$$\iff U_i(D^*) - U_i(D^* \cup X \cup Y) \leq U_i(D^* \cup X) - U_i(D^* \cup X \cup Y) + U_i(D^* \cup Y) - U_i(D^* \cup X \cup Y)$$

$$\iff U_i(D^*) - U_i(D^* \cup X \cup Y) \leq L_i(Y) + L_i(X)$$

$$\iff L_i(X \cup Y) \leq L_i(X) + L_i(Y).$$

The last inequality and the submodularity of $\Pi$ imply that the total compensation is lower and the total revenue of intermediaries is greater in an equilibrium corresponding to a coarser partition. As all equilibria in Proposition 5 have the same total surplus, we obtain the desired result. \hfill \square
7.2 Information Design by Competing Data Intermediaries

I use the above results to study information design by competing data intermediaries. I assume that a downstream firm is a seller that uses consumer data for product recommendation and price discrimination. Each piece of data \( d \in D_i \) is an informative signal about consumer \( i \)'s willingness to pay. Intermediaries can potentially obtain any signals from consumers.

The formal description is as follows. Assume for simplicity that there is a single consumer (thus, omit subscript \( i \)). I now label a downstream firm as a seller. The seller sells \( M \in \mathbb{N} \) products \( 1, \ldots, M \). The consumer has a unit demand, and her values for products, \( u := (u_1, \ldots, u_M) \), are independently and identically distributed according to a cumulative distribution function \( F \) with a finite support \( V \subset (0, +\infty) \).

The consumer has a set of data \( D \), where each \( d \in D \) is a signal (Blackwell experiment) from which the seller can learn about \( u \). I assume that \( D \) consists of all signals with finite realization spaces.

After buying data \( D \subset D \) from intermediaries, the seller learns about values \( u \) from signals in \( D \). Then, the seller sets a price and recommends one of \( M \) products to the consumer. Finally, the consumer observes the value and the price of the recommended product, and she decides whether to buy it. A recommendation could be an advertiser displaying a targeted advertisement or an online retailer showing a product as a personalized recommendation. The consumer’s payoff from this transaction is \( u_m - p \) if she buys product \( m \) at price \( p \); Otherwise, her payoff is zero. The seller’s payoff is its revenue. In any subgame where the seller has obtained data \( D \), I consider pure-strategy perfect Bayesian equilibrium such that the seller calculates its posterior belief based on the prior \( F \) and signals in \( D \) on and off the equilibrium paths.

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13 I define \( F \) as a left-continuous function. Thus, \( 1 - F(p) \) is the probability that the consumer’s value for any given product is weakly greater than \( p \) at the prior.

14 To close the model, I need to specify how realizations of different signals are correlated conditional on \( u \). One way is to use the formulation of Gentzkow and Kamenica (2017): Let \( X \) be a random variable that is independent of \( u \) and uniformly distributed on \([0, 1]\) with typical realization \( x \). A signal \( d \) is a finite partition of \( V^M \times [0, 1] \), and the seller observes a realization \( s \in d \) if and only if \((v, x) \in s \). However, the result does not rely on this particular formulation.

15 The model assumes that the seller only recommends one product, and thus the consumer cannot buy non-recommended products. This captures the restriction on how many products can be marketed to a given consumer. See Ichihashi (2019) for a detailed discussion of the motivation behind this formulation.

16 I assume that the seller breaks ties in favor of the consumer. The existence of an equilibrium is shown in Ichihashi (2019).
An important observation is that total surplus is maximized when the seller has all data, and thus Assumption 4 holds. Indeed, if the seller has all data \( D \), it can perfectly learn \( u \) because \( D \) contains a fully informative signal. Then, the seller can recommend the highest value product and perfectly price discriminate the consumer, which maximizes total surplus.

I prepare several notations. Given a set \( D \) of signals, let \( U(D) \) and \( \Pi(D) \) denote the expected payoffs of the consumer and the seller, respectively, when the seller that has \( D \) optimally sets a price and recommends a product, and the consumer makes an optimal purchase decision. Note that \( \Pi(D) \) is increasing because a larger \( D \) corresponds to a more informative signal. Define

\[
p(F) := \min(\arg \max_{p \in V} p[1 - F(p)])
\]

as the lowest monopoly price given a value distribution \( F \).

A monopoly intermediary obtains the efficient amount of information (such as a fully informative signal) and extracts full surplus from the consumer and the seller. Thus, consumer surplus is \( U(\emptyset) \), the payoff in a hypothetical scenario where the seller recommends one of \( M \) products randomly at a price of \( p(F) \). In contrast, if the market consists of multiple intermediaries, consumer surplus can be equal to the one in a hypothetical scenario where the consumer chooses what information to disclose to the seller. In other words, consumer surplus is equal to the one in Bayesian persuasion (see Appendix J for the proof).

**Proposition 7.** Suppose that there are multiple intermediaries. In the partially monopolistic equilibrium, one intermediary (say 1) obtains a fully informative signal, and the consumer obtains a payoff of \( \max_{d \in D} U(d) \). Moreover, this equilibrium satisfies the following.

1. If the seller sells a single product, all intermediaries earn zero payoffs. The consumer obtains payoff \( U(d^*) \), where \( d^* \) is the consumer-optimal segmentation in Bergemann et al. (2015).

2. Suppose that the seller sells multiple products. For a generic prior \( F \) satisfying \( p(F) > \min V > 0 \), intermediary 1 earns a positive payoff that is independent of the number of intermediaries.\(^{17}\)

\(^{17}\)A generic \( F \) means that the statement holds for any probability distribution in \( \Delta(V) \subset \Delta(\mathbb{R}^M) \) satisfying \( p(F) > \min V \), except for those that belong to some Lebesgue measure-zero subset of \( \Delta(V) \).
The intuition is as follows. First, consider the single product case (Point 1). Bergemann et al. (2015) show that there is a signal $d^*$ such that (i) $d^*$ maximizes the consumer’s payoff, i.e., $d^* \in \arg \max_{d \in D} U(d)$, (ii) the seller is indifferent between obtaining $d^*$ and nothing, i.e., $\Pi(d^*) = \Pi(\emptyset)$, and (iii) $d^*$ maximizes total surplus $U(d) + \Pi(d)$. (i) implies that competing intermediaries cannot charge the consumer a positive fee for $d^*$. (ii) implies that they cannot charge the firm a positive price for $d^*$. Moreover, (iii) implies that intermediaries cannot make a profits by obtaining and selling additional information. Thus, in an equilibrium where $d^*$ is obtained and sold, no intermediaries can make a positive profit. In this case, competition among intermediaries yields the consumer all welfare gain from her information.

Second, consider the multiple product case (Point 2). Ichihashi (2019) shows that whenever the prior $F$ satisfies the condition in Point 2, any signal $d^*$ that maximizes the consumer’s payoff $U(d)$ leads to inefficiency. Intuitively, $d^*$ garbles the information about which product is most valuable to the consumer. While this benefits the consumer by inducing the seller to lower prices, it leads to inefficiency due to an inaccurate product recommendation. This creates a room for competing intermediaries to earn a positive profit: An intermediary can additionally obtain information from which the seller can perfectly learn the highest value product and the consumer’s willingness to pay. The consumer requires a positive compensation to share such information. This, in turn, implies that a single intermediary can act as a monopoly of the information. Therefore, the presence of intermediaries are welfare-enhancing relative to Bayesian persuasion, and intermediary surplus could be positive for any number of intermediaries in the market.

8 Extensions

8.1 Multiple Downstream Firms

The model can readily take into account multiple downstream firms if they do not interact with each other: Suppose that there are $L$ firms, where firm $\ell \in L$ has revenue function $\Pi^\ell$ that depends only on data available to $\ell$. Each consumer $i$’s utility of sharing data is $\sum_{\ell \in L} U^\ell_i$, where each $U^\ell_i$ depends on the set of $i$’s data that firm $\ell$ obtains.

This setting is equivalent to the one with a single firm. First, Lemma 1 implies that each
intermediary $k$ posts a price of $\Pi_\ell(\cup_k D^k) - \Pi_\ell(\cup_{j\neq k} D^k)$ to firm $\ell$ in the downstream market. Note that I implicitly assume that intermediaries can price discriminate firms.

Given the pricing rule, the revenue of intermediary $k$ given the allocation of data $(D^k)_k$ is $\sum_{\ell \in L} [\Pi_\ell(\cup_k D^k) - \Pi_\ell(\cup_{j\neq k} D^k)]$. By setting $\Pi := \sum_{\ell \in L} \Pi_\ell$, we can calculate the equilibrium revenue of each intermediary in the downstream market as in Lemma 1.

Second, intermediaries cannot commit to not sell data to downstream firms. Thus, once a consumer shares her data with one intermediary, the data is sold to all firms. This means that in equilibrium, each consumer $i$ decides which offers to accept in order to maximize total compensation plus $\sum_{\ell \in L} U_\ell^i(D_i)$. Therefore, by setting $U_i := \sum_{\ell \in L} U_\ell^i$, we can apply the same analysis as before.

### 8.2 Privacy Concern Toward Data Intermediaries

Consumers may incur exogenous costs of sharing data not only with downstream firms but also with data intermediaries. I can incorporate this by assuming that each consumer incurs a loss of $\rho K_i$ by sharing her data with $K_i$ intermediaries.

For the case of single unit data (Subsection 6.1), the result does not change qualitatively. If $\rho > 0$, intermediaries obtain less data than the original model, because it has to pay a compensation of at least $C_i + \rho$ to each consumer. Any equilibrium allocation of data is partitional, and there are multiple equilibria, one of which is a monopoly equilibrium.

### 8.3 Informational Externality Among Consumers

So far, I have assumed that each consumer’s gross payoff $U_i$ is independent of what data the downstream firm has on other consumers. However, this assumption may fail, for instance, if the firm uses other consumer’s data to infer a consumer’s willingness to pay and use the inference to price discriminate her. For another instance, $U_i$ would depend on other consumer’s data if the firm chooses a single action such as a price or a product design based on the aggregate data, as in Bergemann and Bonatti (2019).

The model can incorporate such dependency (which I call informational externality) by writing $U_i$ as $U_i(D_i, D_{-i})$, where $D_i \subset D_i$ and $D_{-i} \subset \cup_{j \in N \setminus \{i\}} D_j$. Suppose that $U_i(D_i, D_{-i})$ satisfies
assumptions (such as submodularity) in the previous sections for any given $D_{-i}$. Then, all the results continue to hold under the additional assumption that each consumer does not observe offers made to other consumers. To see why we need this assumption, suppose that offers are publicly observable and intermediary $k$ makes a deviating offer to consumer $i$. When $U_j$ depends on what data the firm will have on consumer $i$, then this deviation may affect the data-sharing decision of consumer $j \neq i$ to intermediary $\ell \neq k$. In this case, intermediaries may not be able to sustain a monopoly outcome since each intermediary may fail to internalize how its deviation affect other intermediaries.

Finally, if informational externalities exist, the monopoly equilibrium may be inefficient because a monopolist can use compensation that does not reflect externalities among consumers. This is one of the insights in Bergemann and Bonatti (2019).

9 Conclusion

This paper studies competition among data intermediaries, which obtain data from consumers and sell them to downstream firms. The model incorporates two key features of personal data: One is that data are non-rivalrous, and the other is that the use of data by third parties could affect consumers. These features drastically change the nature of competition relative to the intermediation of physical goods: When the firm’s use of data hurts consumers, data intermediaries may secure monopoly profit in some equilibrium, and the equilibrium allocation of data across intermediaries is not unique. This enables me to compare equilibria with different degrees of data concentration. Under a certain condition, an equilibrium with greater data concentration is associated with higher profits of intermediaries and lower consumer welfare. The main insights hold even when consumers have heterogeneous and arbitrary preferences over the firm’s use of data: Intermediaries compete for data that consumers would voluntarily share with the firm, and a single intermediary acts as a monopsony of data for which consumers would require compensation.
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**Appendix**

**A Proof of Claim 2**

Below, I write $X - Y$ to mean $X \setminus Y$, and $X - Y - Z$ to mean $(X \setminus Y) \setminus Z$. Take any $K \geq 2$ and suppose to the contrary that there is an equilibrium in which one intermediary, say 1, obtains a positive payoff. Suppose that each intermediary $k$ obtains data $D^k_i$ from consumer $i \in N^k$ at compensation $\tau^k_i$. Define $D^* := \bigcup_k D^k$. Suppose that intermediary 2 deviates and offers each consumer $i \in N^1$ an offer of $(D^1_i \cup D^2_i, \tau^1_i + \tau^2_i + \varepsilon)$. Then, all consumers in $N^1$ accept the offer of intermediary 2 but not 1. In the downstream market, the revenue of intermediary 2 increases from $\Pi(D^*) - \Pi(D^* - D^2)$ to $\Pi(D^*) - \Pi(D^* - D^1 - D^2)$, which yields a net gain of $\Pi(D^* - D^2) - \Pi(D^* - D^1 - D^2)$. By *Assumption 1*, $\Pi(D^* - D^2) - \Pi(D^* - D^1 - D^2) > 0$ for a small $\varepsilon > 0$. Thus, intermediary 2 has a profitable deviation, which is a contradiction.

Second, suppose to the contrary that there is an equilibrium where the firm obtains a positive payoff. This means that multiple intermediaries obtain different non-empty data. If $\Pi(\bigcup_k D^k) = \sum_{k \in K} \Pi(D^k)$, then the firm’s payoff would be zero. Thus, $\Pi(\bigcup_k D^k) > \sum_{k \in K} \Pi(D^k)$ holds. This implies that, in the upstream market, an intermediary can unilaterally deviate and increase its payoff by offering slightly higher compensation to consumers in order to obtain $\bigcup_{k \in K} D^k$. This is a contradiction, and thus the firm obtains a payoff of zero. This argument also implies that, if $\Pi$ is strictly supermodular, in any equilibrium, there is at most one intermediary that obtains non-empty data.
**B Proof of Lemma 1**

*Proof.* Take any allocation of data \((D^1, \ldots, D^K)\). I show that the equilibrium revenue of each intermediary \(k\) is at most \(\Pi^k\). Suppose to the contrary that (without loss of generality) intermediary 1 obtains a strictly greater revenue than \(\Pi^1\). Let \(K' \ni 1\) denote the set of intermediaries from which the firm buys data.

First, in equilibrium, \(\Pi(\bigcup_{k \in K'} D^k) = \Pi(\bigcup_{k \in K} D^k)\). To see this, note that if \(\Pi(\bigcup_{k \in K'} D^k) < \Pi(\bigcup_{k \in K} D^k)\), then there is some \(\ell \in K\) such that \(\Pi(\bigcup_{k \in K'} D^k) < \Pi(\bigcup_{k \in K'} \cup \{\ell\} D^k)\). Such intermediary \(\ell\) can profitably deviate by setting a sufficiently low positive price, because the firm then buys data \(D^\ell\). This is a contradiction.

Second, define \(K^* := \{\ell \in K : \ell \not\in K', p^\ell = 0\} \cup K'\). Note that \(K^*\) satisfies \(\Pi(\bigcup_{k \in K'} D^k) = \Pi(\bigcup_{k \in K} D^k)\), \(\sum_{k \in K'} p^k = \sum_{k \in K^*} p^k\), and \(p^j > 0\) for all \(j \not\in K^*\).

It holds that

\[
\Pi(\bigcup_{k \in K^*} D^k) - \sum_{k \in K^*} \hat{p}^k = \max_{J \subset K \setminus \{1\}} \left( \Pi(\bigcup_{k \in J} D^k) - \sum_{k \in J} \hat{p}^k \right).
\]  

(8)

To see this, suppose one side is greater than the other. If the left hand side is strictly greater, then intermediary 1 can profitably deviate by slightly increasing its price. If the right hand side is strictly greater, then the firm would not buy \(D^1\). In either case, we obtain a contradiction.

Let \(J^*\) denote a solution of the right hand side of (8). I consider two cases. First, suppose that there exists some \(j \in J^* \setminus K^*\). By the construction of \(K^*\), \(p^j > 0\). Then, intermediary \(j\) can profitably deviate by slightly lowering \(p^j\). To see this, note that

\[
\Pi(\bigcup_{k \in K} D^k) - \sum_{k \in K^*} \hat{p}^k < \Pi(\bigcup_{k \in J^*} D^k) - \sum_{k \in J^*} \hat{p}^k,
\]

(9)

where \(\hat{p}^k = p^k\) for all \(k \neq j\) and \(\hat{p}^j = p^j - \varepsilon > 0\) for a small \(\varepsilon > 0\). This implies that after the deviation by intermediary \(j\), the firm buys data \(D^j\). This is because the left hand side of (9) is the maximum revenue that the firm can obtain if it cannot buy data \(D^j\), and the right hand side is the lower bound of the revenue that the firm can achieve by buying \(D^j\). Thus, the firm always buy data \(D^j\), which is a contradiction.

Second, suppose that \(J^* \setminus K^* = \emptyset\), i.e., \(J^* \subset K^*\). This implies that the right hand side of (8) can
be maximized by $J^* = K^* \setminus \{1\}$, because $\Pi$ is submodular and $\Pi(\cup_{k \in K^* \setminus \{\ell\}} D^k) \geq p^\ell$ for all $\ell \in K^*$. Plugging $J^* = K^* \setminus \{1\}$, we obtain

$$\Pi(\cup_{k \in K} D^k) - \sum_{k \in K^*} p^k = \Pi(\cup_{k \in K^* \setminus \{1\}} D^k) - \sum_{k \in K^* \setminus \{1\}} p^k. \quad (10)$$

I show that there is $j \not\in K^*$ such that

$$\Pi(\cup_{k \in K^* \setminus \{1\}} D^k) < \Pi(\cup_{k \in (K^* \setminus \{1\}) \cup \{j\}} D^k). \quad (11)$$

Suppose to the contrary that for all $j \not\in K^*$,

$$\Pi(\cup_{k \in K^* \setminus \{1\}} D^k) = \Pi(\cup_{k \in (K^* \setminus \{1\}) \cup \{j\}} D^k). \quad (12)$$

By submodularity, this implies that

$$\Pi(\cup_{k \in K^* \setminus \{1\}} D^k) = \Pi(\cup_{k \in K \setminus \{1\}} D^k).$$

Then, we can write (10) as

$$\Pi(\cup_{k \in K} D^k) - \sum_{k \in K^*} p^k = \Pi(\cup_{k \in K \setminus \{1\}} D^k) - \sum_{k \in K^* \setminus \{1\}} p^k$$

which implies $\Pi^1 = p^1$, a contradiction. Thus, there must be $j \not\in K^*$ such that (11) holds. Such intermediary $j$ can again profitably deviate by lowering its price, which is a contradiction. Therefore, intermediary $k$’s revenue is at most $\Pi^k$.

Finally, I show that in equilibrium, each intermediary $k$ gets a revenue of at least $\Pi^k$. This follows from the submodularity if $\Pi$: If intermediary $k$ sets a price of $\Pi^k - \varepsilon$, the firm buys $D^k$ no matter what prices other intermediaries set. Thus, intermediary $k$ must obtain a payoff of at least $\Pi^k$ in equilibrium. Combining this with the previous part, we can conclude that in any equilibrium, each intermediary $k$ obtains a revenue of $\Pi^k$. \qed
C Proof of Proposition 1

Proof. Suppose to the contrary that there is an equilibrium in which multiple intermediaries, say 1 and 2, obtain the same piece of data \( d_i \). Since consumer \( i \) prefers to share her data, the sum of compensations from intermediaries 1 and 2 is at least \( C_i > 0 \). This implies that at least one intermediary, say 1, pays a positive compensation to consumer \( i \). However, intermediary 1 can increase its payoff by offering \((\emptyset, 0)\) to consumer \( i \). By Corollary 1, this does not reduce intermediary 1’s revenue in the downstream market. Moreover, it reduces intermediary 1’s expense in the upstream market. This is a contradiction. Note that my solution concept ensures that intermediary 1’s deviation with respect to consumer \( i \) does not affect other consumer’s data sharing decisions. □

D Proof of Theorem 1

Proof. Take any partitional allocation of data \((D^1, \ldots, D^K)\) with \( \cup_{k \in K} D^k = D^M \). Let \( N^k \) denote the set of consumers from whom intermediary \( k \) obtains data. Consider the following strategy profile: If \( d_i \in D^k \), intermediary \( k \) offers \((d_i, C_i)\) to consumer \( i \). Otherwise, it offers \((\emptyset, 0)\). In the downstream market, intermediaries set prices according to Lemma 1. The off-path behaviors of consumers are as follows. Suppose that a consumer detects a deviation by any intermediary. Then, the consumer accepts a set of offers to maximize her payoff, but here, the consumer accepts an offer if she is indifferent between accepting and rejecting it.

First, all consumers are indifferent between accepting and rejecting the offers, and thus it is optimal for them to accept all non-empty offers. Second, intermediaries and the firm have no profitable deviation in the downstream market by Lemma 1. Third, suppose that intermediary \( k \) unilaterally deviates in the upstream market and offers \((D^k_i, \tau^k_i)\) to each consumer \( i \). Note that we can without loss of generality focus on offers such that \((D^k_i, \tau^k_i) = (\emptyset, 0)\) for all \( i \in \cup_{j \neq k} N^j \). Indeed, if \( k \) pays a positive compensation to consumer \( i \in N^j \), consumer \( i \) also accepts the offer of intermediary \( j \). By Corollary 1, this does not increase intermediary \( k \)’s revenue. Let \( D^{-k} := \cup_{j \neq k} D^j \) denote the data held by intermediaries other than \( k \). Let \( \hat{D}^k \subset D \setminus D^{-k} \) denote the data that intermediary \( k \) obtains as a result of the deviation. If this deviation is strictly profitable for \( k \), it holds that \( \Pi(\hat{D}^k \cup D^{-k}) - \Pi(D^{-k}) - \sum_{d \in \hat{D}^k} C_i(d) > \Pi(D^k \cup D^{-k}) - \Pi(D^{-k}) - \sum_{d \in D^k} C_i(d) \). However, this never holds because the monopolist could then earn strictly higher
revenue by obtaining and selling $\hat{D}^k \cup D^{-k}$ instead of $D^M$, which is a contradiction. \hfill \square

E \quad \textbf{Proof of Theorem 3}

\begin{proof}
Suppose that each intermediary $k$ offers $(D^k_i, \tilde{\tau}^q_i)$ to each consumer $i$ and sets a price of data following Lemma 1. I show that this strategy profile is an equilibrium. First, Lemma 1 implies that there is no profitable deviation in the downstream market. Second, suppose that intermediary $k$ deviates and offers $(\hat{D}^k_i, \tilde{\tau}^q_i)$ to each consumer $i$. Without loss of generality, we can assume that $\hat{D}^k_i \subset D^k_i$. The reason is as follows. If consumer $i$ rejects $(\hat{D}^k_i, \tilde{\tau}^q_i)$, intermediary $k$ replace it with $(\hat{D}^k_i, \tilde{\tau}^q_i) = (0, 0)$. If consumer $i$ accepts $(\hat{D}^k_i, \tilde{\tau}^q_i)$ but $\hat{D}^k_i \subset D^k_i$, it means that intermediary $k$ obtains some data $d \in \hat{D}^k_i \setminus D^k_i$. Because $\cup_k D^k = D^M = \mathcal{D}$, there is another intermediary that obtains data $d$. By Corollary 1, intermediary $k$ is indifferent between offering $(\hat{D}^k_i \setminus \{d\}, \tilde{\tau}^q_i)$ and offering $(\hat{D}^k_i, \tilde{\tau}^q_i)$. Let $D^- := D^k \setminus \hat{D}^k_i$ denote the set of data that are not acquired by the firm as a result of intermediary $k$’s deviation. If intermediary $k$ deviates in this way, its revenue in the downstream market decreases by $\Pi(D^M) - \Pi(D^M \setminus D^-) - \Pi(D^M \setminus D^k) = \Pi(D^M) - \Pi(D^M - D^-)$. In the upstream market, if consumer $i$ provides data $\hat{D}^k_i$ to intermediary $k$, then it is optimal for consumer $i$ to accept other offers from non-deviating intermediaries, because $C_i$ is supermodular. This implies that the minimum compensation that intermediary $k$ has to pay is $C_i(D_i \setminus D^-_i) - C_i(D_i \setminus D^k_i)$. Thus, intermediary $k$’s compensation to consumer $i$ in the upstream market decreases by $C_i(D_i) - C_i(D_i \setminus D^k_i) - [C_i(D_i \setminus D^-_i) - C_i(D_i \setminus D^k_i)] = C_i(D_i) - C_i(D_i \setminus D^-_i)$. Thus, $k$’s total compensation decreases by $\sum_{i \in \mathcal{N}} [C_i(D_i) - C_i(D_i \setminus D^-_i)]$. Because $D^M = \mathcal{D}$ is an optimal choice of the monopolist, it holds that $\Pi(D^M) - \Pi(D^M \setminus D^-) - \sum_{i \in \mathcal{N}} [C_i(D_i) - C_i(D_i \setminus D^-_i)] \geq 0$. Therefore, the deviation does not increase intermediary $k$’s payoff. \hfill \square

F \quad \textbf{Proof of Theorem 4}

\begin{proof}
Let $(\hat{D}_k)_{k \in K}$ and $(D_k)_{k \in K}$ denote two partitional allocations of data such that the former is more concentrated than the latter. Without loss of generality, assume that $\cup_k \hat{D}^k = \cup_k D^k = \mathcal{D}$. 37
Note that in general, for any set \( S_0 \subset S \) and a partition \((S_1, \ldots, S_K)\) of \( S_0 \), we have
\[
\Pi(S) - \Pi(S - S_0) = \Pi(S) - \Pi(S - S_1) + \Pi(S - S_1) - \Pi(S - S_1 - S_2) + \cdots + \Pi(S - S_1 - S_2 - \cdots - S_{K-1}) - \Pi(S - S_1 - S_2 - \cdots - S_K) \\
\geq \sum_{k \in K} \left[ \Pi(S) - \Pi(S - S_k) \right],
\]
where the last inequality follows from the submodularity of \( \Pi \). For any \( \ell \in K \), let \( K(\ell) \subset K \) satisfy \( \hat{D}^\ell = \sum_{k \in K(\ell)} D^k \). The above inequality implies
\[
\Pi(D) - \Pi(D - \hat{D}^\ell) \geq \sum_{k \in K(\ell)} \left[ \Pi(D) - \Pi(D - D^k) \right], \forall \ell \in K
\Rightarrow \sum_{\ell \in K} \left[ \Pi(D) - \Pi(D - \hat{D}^\ell) \right] \geq \sum_{\ell \in K} \sum_{k \in K(\ell)} \left[ \Pi(D) - \Pi(D - D^k) \right].
\]
In the last inequality, the left and the right hand sides are the total revenue for intermediaries in the downstream market under \((\hat{D}^k)\) and \((D^k)\), respectively. We can prove the result on consumer surplus by replacing \( \Pi \) with \(-C_i\). Note that if \((\hat{D}^k)\) is more concentrated than \((D^k)\), \((\hat{D}^k_i)\) is more concentrated than \((D^k_i)\).

**G Proof of Proposition 3**

*Proof.* Consider the following strategy profile: In the upstream market, intermediary 1 offers \((D_i, U(D_i^*) - U(D_i))\) to each consumer \( i \). Other intermediaries offer \((D_i^*, 0)\) to each consumer \( i \). Consumers accept only the offer of intermediary 1. If an intermediary deviates, then consumers optimally decide which intermediaries to share data with, breaking ties in favor of sharing data. In the downstream market, if intermediary 1 does not deviate in the upstream market, then any intermediary \( j \neq 1 \) sets a price of zero, and intermediary 1 sets a price of \( \Pi(D) - \Pi(D^{-1}) \), where \( D^{-1} \) is the set of data that intermediaries other than 1 hold. If intermediary 1 deviates in the upstream market, then assume that players play any equilibrium of the corresponding subgame.

I show that the suggested strategy profile consists of an equilibrium. First, I show that intermediary 1 has no incentive to deviate. Suppose that intermediary 1 deviates and obtains data.
$D_i$ from each consumer $i$. Let $\hat{D}_i$ denote the set of all data that consumer $i$ shares as a result of 1’s deviation ($D_i \subset \hat{D}_i$ if consumer $i$ also shares data with some intermediary $j \neq 1$). The revenue of intermediary 1 in the downstream market is at most $\Pi(\bigcup_{i \in N} \hat{D}_i)$. The compensation to each consumer $i$ has to be at least $\tau_i \geq U(D_i) - U(\hat{D}_i)$. To see this, suppose $U(D_i) > U(\hat{D}_i) + \tau_i$. The left hand side is the payoff that consumer $i$ can attain by sharing data exclusively with intermediary $k > 1$. The right hand side is her maximum payoff conditional on sharing data with intermediary 1. Note that all intermediaries other than 1 offer zero compensation. Then, $U(D_i) > U(\hat{D}_i) + \tau_i$ implies that consumer $i$ would strictly prefer to accept an offer of intermediary $k \neq 1$. Now, these bounds on revenue and cost imply that intermediary 1’s payoff after the deviation is at most $\Pi(\bigcup_{i \in N} \hat{D}_i) - \sum_{i \in N} [U_i(D_i) - U_i(\hat{D}_i)] = \Pi(\bigcup_{i \in N} \hat{D}_i) + \sum_{i \in N} U_i(\hat{D}_i) - \sum_{i \in N} U_i(D_i)$. Since the efficient outcome involves full data sharing, this is at most $\Pi(\bigcup_{i \in N} D_i) + \sum_{i \in N} U_i(D_i) - \sum_{i \in N} U_i(D_i) = \Pi(\bigcup_{i \in N} D_i) - \sum_{i \in N} [U_i(D_i) - U_i(D_i)]$, which is intermediary 1’s payoff without deviation. Thus, there is no profitable deviation for intermediary 1.

Second, suppose that intermediary 2 deviates and offers $(D_i^2, \tau_i^2)$ to each consumer $i$. Without loss of generality, assume that each consumer accepts the offer. Let $D_i^{-1}$ denote the set of data that consumer $i$ provides to intermediaries in $K \setminus \{1\}$ after the deviation. If the consumer accepts the offer of intermediary 1, her payoff increases by $U_i(D_i) - U_i(D_i^{-1}) + U_i(D_i^2) - U_i(D_i) \geq U_i(D_i) - U_i(D_i^2) + U_i(D_i^2) - U_i(D_i) = 0$. The inequality follows from $U_i(D_i^2) \geq U_i(D_i^{-1})$. Thus, each consumer $i$ prefers to accept the offer of intermediary 1. If $\tau_i^2 \geq 0$, this implies that intermediary 2’s could be better off (relative to the deviation) by not collecting $D_i^2$, because it can save compensation without losing revenue in the downstream market. Indeed, intermediary 2’s revenue in the downstream market is zero for any increasing $\Pi$. If $\tau_i^2 < 0$, consumer $i$ strictly prefers sharing data with intermediary 1 to sharing data with intermediary 2. Overall, these imply that intermediary 2 does not benefit from the deviation. 

\[\square\]

**H Proof of Proposition 4**

**Proof.** In the equilibrium of Proposition 3, each consumer obtains a payoff of $U_i(D_i^*)$, intermediary surplus is $\Pi(D) - \sum_{i \in N} U_i(D_i^*)$, and the firm’s payoff is zero. Thus, it suffices to show
that in any equilibrium, each consumer $i$ obtains a payoff of at least $U_i(D^*_i)$. Define $m := \min_{d \in D, D \in \mathcal{D}} \Pi(D) - \Pi(D \setminus \{d\}) > 0$ and $TS^* := \Pi(D) + \sum_{i \in N} U_i(D) > 0$ where $U_i(D) := U_i(D \cap D_i)$. Let $K^*$ satisfy $K^* > TS^*/m$.

Suppose that there are $K \geq K^*$ intermediaries and take any equilibrium. Suppose (to the contrary) that the payoff of consumer $i$ is $U_i(D^*_i) - \delta$ with $\delta > 0$. I derive a contradiction by assuming that any intermediary obtains a payoff of at least $m$. Suppose to the contrary that intermediary $k$ earns a strictly lower payoff than $m$. If intermediary $k$ deviates and offers $(D^*_i, \varepsilon)$ with $\varepsilon \in (0, \delta)$ to consumer $i$, then she accepts this offer. Let $D^{-k}_i$ denote the data that consumer $i$ shares with intermediaries in $K \setminus \{k\}$ as a result of $k$’s deviation. Then, $D^*_i \setminus D^{-k}_i \neq \emptyset$ holds. To see this, suppose to the contrary that $D^*_i \subset D^{-k}_i$. Then, consumer $i$ could be strictly better off by rejecting intermediary $k$’s offer $(D^*_i, \varepsilon)$ because $\varepsilon > 0$. However, conditional on rejecting $k$’s deviating offer, the set of offers that consumer $i$ faces shrinks relative to the original equilibrium. Thus, the maximum payoff the consumer can achieve by rejecting $k$’s deviating offer is at most $U_i(D^*_i) - \delta < U_i(D^*_i) - \varepsilon$, which is a contradiction. Since consumer $i$ accepts the offer of intermediary $k$ and $D^*_i \setminus D^{-k}_i \neq \emptyset$, intermediary $k$ can earn a profit arbitrarily close to $m$ from consumer $i$. This implies that in the equilibrium, any intermediary earns a payoff of at least $m$; otherwise, an intermediary can profitably deviate by offering empty offers to all consumers in $N \setminus \{i\}$ and $(D^*_i, \varepsilon)$ to consumer $i$. However, if each intermediary earns at least $m$, the sum of payoffs of all intermediaries is at least $Km > TS^*$. This implies that one of consumers and the firm obtains a negative payoff, which is contradiction. Therefore, in any equilibrium, any consumer obtains a payoff of at least $U_i(D^*_i)$.

I Proof of Proposition 5

Proof. $L_i(D^k_i)$ in (7) is the maximum loss that consumer $i$ incurs by sharing $D^k_i$ with the firm, where the maximum is taken across all sets of data she shares through other intermediaries. Define $M_i(D^k_i)$ as follows. If $L_i(D^k_i) = 0$, let $M_i(D^k_i) = D_i$, i.e., the set of all data on consumer $i$. If $L_i(D^k_i) > 0$, let $M_i(D^k_i) \in \arg \max_{D \subset \mathcal{D}} U_i(D) - U_i(D \cup D^k_i)$. If there are multiple maximizers, choose any maximizer $D$ such that there is no other maximizer $\tilde{D}$ with $D \subset \tilde{D}$. Such a $D$ exists because $\mathcal{D}$ is finite. Note that $U_i(M_i(D^k_i)) - U_i(M_i(D^k_i) \cup D^k_i) = L_i(D^k_i)$. An important
observation is that $M_i(D^k_i) \supset D^{-1}_i$ where $D^{-1}_i = \bigcup_{k=2}^J D^k_i$ is the set of data consumer $i$ shares with intermediaries other than 1. If $L_i(D^k_i) = 0$, $M_i(D^k_i) \supset D^{-1}_i$ holds because $M_i(D^k_i) = \mathcal{D}_i$. This is also true if $L_i(D^k_i) > 0$. To see this, suppose to the contrary that $M_i(D^k_i) \supset D^{-1}_i$. The submodularity of $U_i$ implies that $U_i(M_i(D^k_i) \cup D') - U_i(M_i(D^k_i) \cup D' \cup D^k_i) \geq L_i(D^k_i)$ where $D' := D^{-1}_i \setminus M_i(D^k_i) \neq \emptyset$. This contradicts the construction of $M_i(D^k_i)$.

Consider the following strategy profile. Each intermediary $k \leq J$ offers $(D^k_i, L_i(D^k_i))$ to each consumer $i$. Each intermediary $k + \ell$ with $\ell \in \{1, \ldots, J\}$ offers $(M_i(D^k_i), 0)$ to consumer $i$. In the downstream market, the behavior of intermediaries and the firm follows Lemma 1. On the path of play, consumers accept offers from intermediaries $1, \ldots, J$ and reject others. Off the path of play, consumers optimally choose the set of offers to accept, breaking ties in favor of accepting an offer.

I show that the above strategy profile consists of an equilibrium. First, each consumer $i$ prefers to accept offer $(D^k_i, L_i(D^k_i))$ on and off the equilibrium paths by the construction of $L_i(D^k_i)$. On the path of play, given that consumer $i$ shares data with intermediaries $1, \ldots, J$, she does not strictly benefit from accepting the offer of intermediary $k > J$. Thus, each consumer has no incentive to deviate.

Any intermediary $j > J$ has no incentive to deviate. To see this, note that consumers continue to accept offers from intermediaries $1, \ldots, J$ after $j$’s deviation. Since $\bigcup_{k=1}^J D^k = \mathcal{D}$, $j$’s deviation does not strictly increase its payoff in the downstream market. Also, $j$ cannot strictly increase its payoff in the upstream market because consumers, who share data $\mathcal{D}$ to intermediaries $1, \ldots, K$, have no incentive to pay to intermediary $j$.

I show that intermediary $k \leq J$ has no incentive to deviate. Suppose that an intermediary (say 1) deviates and offers $(\hat{D}^1_i, \hat{\tau}^1_i)$ to each consumer $i$. Without loss of generality, assume that all consumers accept offers from intermediary 1. Note that consumers continue to accept offers from intermediaries $2, \ldots, J$. Thus, we can assume that $\hat{D}^1_i \subset \mathcal{D} \setminus D^{-1}_i$. Note that intermediary 1’s revenue in the downstream market is $\Pi(D^{-1}_i \cup (\bigcup_{i \in N} \hat{D}^1_i)) - \Pi(D^{-1})$. The compensation $\hat{\tau}^1_i$ to consumer $i$ satisfies $U(D^{-1}_i \cup \hat{D}^1_i) + \hat{\tau}^1_i \geq U(M_i(D^k_i))$. Indeed, if the right hand is strictly greater, then consumer $i$ strictly prefers sharing data with intermediaries $2, \ldots, J, J + 1$ to sharing data with intermediaries $1, \ldots, J$ (here, I use $M_i(D^k_i) \supset \hat{D}^1_i$). Thus, intermediary 1’s payoff from the deviation is at most $\Pi(D^{-1}_i \cup (\bigcup_{i \in N} \hat{D}^1_i)) - \Pi(D^{-1}) + \sum_{i \in N} \left[U(D^{-1}_i \cup \hat{D}^1_i) - U(M_i(D^k_i))\right]$. The sum of the first and third terms, $\Pi(D^{-1}_i \cup (\bigcup_{i \in N} \hat{D}^1_i)) + \sum_{i \in N} U(D^{-1}_i \cup \hat{D}^1_i)$, is maximized at
\hat{D}_i = D_i$ by Assumption 4. Thus, the deviating payoff is bounded from above by

\[
\Pi(D) - \Pi(D^{-1}) + \sum_{i \in N} \left[ U(D_i) - U(M_i(D^k_i)) \right],
\]

which is intermediary 1’s payoff on the path of play. Thus, no intermediary has a profitable deviation.

\[ \square \]

J Proof of Proposition 7

Proof. Note that Proposition 3 holds even when $D$ is not finite. Let $d_{FULL}$ denote a fully informative signal. I show Point 1. Assuming that there is a single product ($M = 1$), Bergemann et al. (2015) show that there is a signal $d^*$ that satisfies the following conditions: $d^* \in \arg\max_{d \in D} U(d);$ $\Pi(d^*) = \Pi(\emptyset);$ $d^*$ maximizes total surplus, i.e., $U(d^*) + \Pi(d^*) = U(d_{FULL}) + \Pi(d_{FULL})$. Namely, $d^*$ simultaneously maximizes consumer surplus and total surplus without increasing the seller’s revenue. These properties imply that intermediary 1’s revenue in the downstream market is equal to the compensation it pays in the upstream market: $\Pi(d_{FULL}) - \Pi(\emptyset) = \Pi(d_{FULL}) - \Pi(d^*) = U(d^*) - U(d_{FULL})$. Thus, all intermediaries earn zero payoffs.

I show Point 2. Ichihashi (2019) shows that if $M = 2$, then for a generic $F$ satisfying $p(F) > \min V$, any signal $d^{**} \in \arg\max_{d \in D} U(d)$ leads to an inefficient outcome. This implies $\Pi(d_{FULL}) + U(d_{FULL}) > \Pi(d^{**}) + U(d^{**}) \geq \Pi(\emptyset) + U(d^{**})$. Then, $\Pi(d_{FULL}) - \Pi(\emptyset) - [U(d^{**}) - U(d_{FULL})] > 0$. Thus, intermediary 1 earns a positive profit.

\[ \square \]